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Investigation into the thermodynamics and kinetics of the binding of Cu$^{2+}$ and Pb$^{2+}$ to TiS$_2$ nanoparticles synthesized using a solvothermal process.

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Highlights
- A TiS$_2$ nanomaterial was synthesized through a solvothermal process
- The binding of Cu$^{2+}$ and Pb$^{2+}$ ions from aqueous solution to the TiS$_2$ was pH dependent
- Lead bound by chemisorption copper bound by a combination of chemi/physi sorption
- Hard cations showed little to no effect on the binding of Pb$^{2+}$ ions to TiS$_2$
- Hard cations affected Cu$^{2+}$ ion binding to TiS$_2$

Abstract
In the present study, titanium (IV) sulfide (TiS$_2$) was synthesized and investigated for the removal of Cu$^{2+}$ and Pb$^{2+}$ ions from aqueous solutions. TiS$_2$ nanoparticles synthesized through a solvothermal synthesis were characterized using x-ray diffraction (XRD) and scanning electron microscopy (SEM). The average particle size for the TiS$_2$ material was determined to be 8.03 ± 0.98 nm from the diffraction pattern. Studies were performed to examine the effects of pH, temperature, time, and interfering ions on the binding of Cu$^{2+}$ and Pb$^{2+}$ to the TiS$_2$. As well isotherm studies were performed to determine the binding capacity of TiS$_2$ for both Cu$^{2+}$ and Pb$^{2+}$ ions. The pH profile studies showed optimal binding occurred at pH 2 for the sorption of both Cu$^{2+}$ and Pb$^{2+}$ to the TiS$_2$. The isotherm studies showed the adsorption capacities at
temperatures of 4, 22, and 45°C for Cu\textsuperscript{2+} were 243, 222, and 153 mg/g, respectively. An opposite trend in the adsorption was observed for Pb\textsuperscript{2+} binding to the TiS\textsubscript{2}. The observed binding capacities for Pb\textsuperscript{2+} were 32, 166, and 357 mg/g, at temperatures of 4, 22, and 45°C, respectively. The thermodynamic parameters for binding showed a non-spontaneous process for the sorption of Cu\textsuperscript{2+} whereas a spontaneous binding process was observed for the sorption of Pb\textsuperscript{2+}.

Additionally, the binding of Cu\textsuperscript{2+} on TiS\textsubscript{2} in the presence of interfering ions (Na\textsuperscript{+}, K\textsuperscript{+}, Mg\textsuperscript{2+}, and/or Ca\textsuperscript{2+}) was observed to decrease at high concentrations; however, the binding of Pb\textsuperscript{2+} was unaffected by the presence of the same cations.

Keywords: Copper sorption, Lead sorption, TiS\textsubscript{2}, Isotherms, Kinetics,
Introduction:

Pollution is caused when harmful or hazardous substances are introduced into the environment. Industrialization has caused the discharge of both biodegradable and non-biodegradable pollutants into the environment. These pollutants can either be organic or inorganic compounds. Heavy metals fall under the classification of non-biodegradable pollutants, which are compounds that are not decomposed or broken down and are thus persistent in the environment. Furthermore, pollution is mobile in the environment and can enter water systems, which may directly affect potable water sources. In recent years, potable water has become a global concern for both human and environmental health. The contamination of potable water can occur through anthropogenic processes such as the synthesis and application of pesticides, petroleum refining by-products and use, fertilizers synthesis and application, as well as other industrial processes. Two elements, which are non-biodegradable pollutants, copper and lead are of interest due to their high number of industrial uses and the health issues upon exposure.

Most copper and lead contamination can generally be attributed to industrial processes such as: paint manufacturing, metal smelting, battery manufacturing, oil refining processes, and mining [1-3]. Improper disposal of contaminated waste, with lead or copper, can lead to the contamination potable water sources. Interestingly, copper is both an essential trace element that is required in low concentrations for growth and development, however, copper can also be considered a toxin [4]. In high amounts, Cu^{2+} primarily leads to liver toxicity but it also causes lesions to the nervous system, diarrhea, abdominal pain, lethargy, and anorexia [1, 5-7]. Lead on the other hand, has no known biological function in the human body. Contact with lead has been shown to affect the production of heme, the nervous system, and the renal system. Lead has been shown to compete with the uptake of calcium in cells as well as calcium binding with
phosphokinase C, which has been shown to effect neural signaling [8]. Exposure to lead readily affects children in developmental stages, since they are in a constant state of growth [9-10].

Current remediation methods for heavy metal ions from aqueous solutions include: biosorption, adsorption, extraction, precipitation, phytoremediation, and ion exchange [11-13]. Although these methods are effective for the removal of heavy metal ions, many of these techniques are either very costly or difficult to implement. For example, ion exchange involves the use of expensive resins to exchange either toxic cations or anions with non-toxic ions [12, 14]. In addition, ion exchange techniques are not ion specific, which can increase the operational expense. Alternatively, the use of precipitating agents can be very effective at removing dissolved ions, but there is an added cost for the disposal of the sludge(s) created from the process. The generation and treatment of large amounts of sludge adds additional steps and cost to the treatment process [12]. Additionally, precipitation and flocculation technologies involve the use of chemicals, which must be removed prior to consumption thus close monitoring of the chemical levels are required. On the other hand, adsorption technologies have obtained much scientific attention for the removal of heavy metal ions from water [1-3, 5, 15-20]. In recent years, adsorption technologies have incorporated the use of nanoparticles as adsorbents, which have high surface areas, high reactivities, and high binding capacities to remove contaminants from solutions.

Several nano-adsorbents have been studied to remove heavy metal ions from water solutions. Some examples of adsorbents used in the removal of toxic heavy metals from aqueous solutions are: aluminum oxides, biochar, iron oxides, graphene oxides, iron sulfides, zinc oxides, titanium dioxides, manganese oxides, copper oxides, red mud, as well as other types of materials, [1-3,5,15-20]. Inorganic nano-adsorbents have obtained a lot of interest, recently, due to their
high binding capacities. For example, adsorption results reported by Mahdavi et al., showed that CuO nanoparticles have capacities of 14.2 mg/g for Pb$^{2+}$ and 54.1 mg/g for Cu$^{2+}$, alternatively ZnO has exhibited higher capacities for both Pb$^{2+}$ and Cu$^{2+}$ at 112.7 mg/g and 137.5 mg/g, respectively [18]. Similarly, Tamez et al., showed that Fe$_3$O$_4$ had binding capacities of 37.04 mg/g and 166.67 mg/g for Cu$^{2+}$ and Pb$^{2+}$ ions, respectively [6]. In the same study, Tamez et al, also showed that Fe$_2$O$_3$ had binding capacities of 19.61 mg/g and 47.62 mg/g for Cu$^{2+}$ and Pb$^{2+}$, respectively [1]. According to Fouladgar et al., γ-Al$_2$O$_3$ has a binding capacity of 51.3 mg/g for Cu$^{2+}$ at 25˚C [21]. The anatase polymorph for titanium dioxide has exhibited a binding capacity of 83.12 mg/g (401.14 µmol/g) for the adsorption of Pb$^{2+}$ [22]. Transition metal sulfides nanomaterials have also shown promise in the removal of toxic ions from aqueous solution [23]. Materials such as Fe$_7$S$_8$ and Pyrite based materials have been shown to be successful in the removal of arsenic from aqueous solution.

In the present study Titanium (IV) sulfide (TiS$_2$) was of interest due to its structural properties that give rise to the electronic and chemical behavior of TiS$_2$ [24]. TiS$_2$ nanoparticles may exhibit higher binding capacities than metal oxides due to its layered structure, which allows the intercalation of ions between the layers, as well as its electrochemical behavior. In the present study, TiS$_2$ was synthesized and studied for the removal of Cu$^{2+}$ and Pb$^{2+}$ from aqueous solution. The material was synthesized through a solvothermal process using elemental sulfur, titanium(IV) chloride, with 1-octadecene as the solvent, and at a temperature of 300˚C. The synthesized TiS$_2$ was characterized using x-ray diffraction, which showed the correct phase was synthesized with an average particle size of 8.03 ± 0.98 nm. Various batch studies were performed to determine the effect of pH, temperature, time, thermodynamics parameters, and
common hard cation interferences on the binding process. In addition, the binding capacities of lead and copper to the TiS₂ nanoparticles were determined using isotherm studies.

2.0 Methodology:

2.1 Synthesis of TiS₂ nanoparticles:

The TiS₂ nanomaterial was prepared using a method similar to that described by Prakabar et al. [25]. In brief, the reaction was performed by dissolving 120 mmol of elemental sulfur in 250 mL of 1-octadecene and heating to 300°C. Once the reaction reached 300°C, 20 mmol of titanium (IV) chloride (TiCl₄) was injected into the solution and the reaction was held at 300°C for 30 min. Subsequent to heating, the reaction mixture was cooled to room temperature naturally and filtered using vacuum filtration. The filtrate was washed using a combination of toluene, acetone, and methanol to remove the solvent and any by-products formed during the reaction.

2.2 X-Ray Diffraction Analysis:

The TiS₂ nanomaterial was characterized using X-ray powder diffraction. The diffraction patterns were collected using a Bruker D2 phaser diffractometer equipped with a Co source (kₐ=1.789 Å), an iron filter, and a scintillation counter detector. The reaction product was homogenized using a mortar and pestle and was placed on a sample holder. The diffraction patterns were collected from 10° to 70° (in 2θ) with a step width of 0.05° and a 5s counting time. The diffraction patterns were fitted using the Le Bail fitting procedure in the FullProf software and crystallographic data from the literature [26-28]. The average particle size was determined using a Gaussian fitting of three independent diffraction peaks and Scherer’s equation.
2.3 SEM

Scanning Electron Microscopy (SEM) and Energy Dispersive X-ray Analysis (EDAX) were collected using a Sigma VP Carl Zeiss. The SEM was operated with accelerating voltages between 3.0 and 5.0 kV and a working distance of 5.7 mm.

2.4 pH Batch Study:

pH profile studies were performed to investigate the effect of pH on the binding of Cu$^{2+}$ and Pb$^{2+}$ ions to the TiS$_2$ nanoparticles. The binding study was performed from pH 2 to pH 6 using 300 ppb solutions of Cu$^{2+}$ or Pb$^{2+}$. The pH of the Cu$^{2+}$ and Pb$^{2+}$ solutions was adjusted using either dilute trace metal grade HNO$_3$ or dilute NaOH. 4.0 mL aliquots of the pH-adjusted solutions were transferred into reaction test tubes containing 10 mg of the TiS$_2$ nanomaterial. In addition, control reactions were performed, which contained the pH adjusted metal ion without the TiS$_2$ nanomaterial. Both the reaction and control samples were equilibrated on a nutating mixer for 1 h at room temperature. Subsequent to equilibration, the reaction and control samples were centrifuged at 3,500 RPM for 5 min, the supernatants were decanted into clean test tubes, and stored for further analysis using ICP-OES. All reaction and control samples were performed in triplicate for statistical purposes.

2.5 Binding Capacity/Thermodynamics Studies:

The capacity studies of TiS$_2$ nanoparticles were conducted for Cu$^{2+}$ and Pb$^{2+}$ using solutions with the following concentrations: 0.3, 3, 30, 100, 300, and 1000 ppm. The solutions were pH adjusted to the optimal binding pH of 2, which was previously determined from the pH

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batch study. 4.0 mL aliquots of the reaction solutions were transferred to test tubes containing 10 mg TiS$_2$. As previously mentioned, control samples consisted of the metal ion solution only. Both reaction and control samples were repeated in triplicate for statistical purposes. The samples and controls were equilibrated for 1 h at 4°C, 22°C, and 45°C on a nutating mixer. Subsequent to equilibration, both the reaction and control samples were centrifuged at 3,500 RPM for 5 min, the supernatants were decanted and transferred to clean test tubes and stored for further analysis using ICP-OES.

2.6 Kinetics Study:

Kinetic studies were performed to determine the rate of the reactions for the sorption of Cu$^{2+}$ and Pb$^{2+}$ ion onto the TiS$_2$ nanomaterial. The reactions were performed using solutions consisting of either 30 ppm of Cu$^{2+}$ or Pb$^{2+}$ were pH adjusted to pH 2, as previously mentioned the optimum binding pH, and were reacted with 10 mg of TiS$_2$ at various time intervals. 4.0 mL aliquots of the solutions were transferred to reaction tubes containing 10 mg TiS$_2$. The control samples consisted of the metal ion reaction solution only. All reactions and control samples were performed in triplicate for statistical purposes. The reaction and control samples were equilibrated on a nutating mixer at three temperatures (4°C, 22°C, and 45°C) and at the following time intervals: 15, 30, 60, and 90 min. Subsequent to equilibration, both the reaction and control samples were centrifuged at 3,500 RPM for 5 min and the supernatants were decanted and stored for further analysis using ICP-OES.

2.7 Interference Study:
The removal of Cu$^{2+}$ and Pb$^{2+}$ ions was studied in the presence of hard cations due to the possible interference on the binding process. For the study, Na$^+$, K$^+$, Mg$^{2+}$ and Ca$^{2+}$ were added to 300 ppb Cu$^{2+}$ or Pb$^{2+}$ solutions at various concentrations. The cation concentrations used were: 0.3, 3, 30, 100, 300 and 1000 ppm. Each solution was adjusted to pH 2 and 4.0-mL aliquots were transferred to reaction tubes containing 10 mg of TiS$_2$. The control samples consisted of the mixed metal ion solution without the TiS$_2$ nanomaterial. Both the reaction and control samples were performed in triplicate for statistical purposes. The samples were equilibrated on a nutating mixer for 1 h at room temperature. After equilibration, both the reaction and control samples were centrifuged at 3,500 RPM for 5 min, and the supernatants were decanted and stored for further analysis using ICP-OES.

2.8 ICP-OES Parameters:

ICP-OES analysis was performed using a Perkin Elmer Optima 8300 ICP-OES (Perkin Elmer, Shelton CT) with Winlab32 software. The parameters used for the analysis are shown in Table 1. If samples were found to be outside of the calibration range of the ICP-OES, then the samples were diluted to fall within the calibration range for the instrument. Furthermore, only calibration curves that had correlation coefficients ($R^2$) of 0.99 or better were used to obtain data.

3.0 Results and Discussion:

3.1 X-Ray Diffraction Characterization of the TiS2 nanomaterial:

The diffraction pattern for the synthesized TiS$_2$ nanomaterial is shown in Figure 1. From the pattern, it was determined that the TiS$_2$ nanomaterial was in a trigonal geometry and had the P3M1 space group. The refined lattice parameters: $a=b=3.397$ Å and $c=5.747$ Å with $\alpha=\beta=90^\circ$
and $\gamma=120^\circ$. The $\chi^2$ for the fitting was 0.939, which showed an excellent agreement between the fitting and the experimental data [24, 25]. The diffraction peaks located at: 18.17, 35.14, 36.82, 40.17, 52.08, 48.05, 56.55, 63.77, 66.92, and 68.88 in 2 theta represent the: 001, 002, 100, 011, 101, 012, 102, 003, 110, 111, 013, and the 103 diffraction planes of TiS$_2$, respectively. The diffraction planes were determined using crystallographic data from the literature and the Le Bail fitting procedure in the FullProf software [24-27]. The particle size of the TiS$_2$ was calculated to be $8.03 \pm 0.98$ nm using Scherrer’s equation. The atomic arrangement of TiS$_2$ consists of the titanium ions surrounded octahedrally by 6 sulfur atoms, which are linked together to form 2-D sheets. Furthermore, the structure of TiS$_2$ consists of the stacking of the 2-D layers/sheets, where each layer stacks on top of another and are held together by van der Waals forces [24].

### 3.2 SEM analysis

Figure 2 shows the SEM images and EDS collected for the synthesized TiS$_2$ nanomaterial. Figure 2 A shows a low-resolution SEM image of the synthesized TiS$_2$. As can be seen Figure 2 A, there is a consistency in the size of the synthesized nanoparticles. The morphology of the synthesized TiS$_2$ nanoparticles on the other hand is complex, shown in Figure 2 B. Superficially the morphology of the material could be referred to as a “flower”. However, the particles are collections of TiS$_2$ platelets, which gives the appearance of the flower morphology. From the image can also be observed that there are at least two different planes present in the sample, there are edge planes and basal planes. The edge plane occurs at the termination of the basal planes. In the SEM image the edge planes are very small approximately 10 nm whereas the basal planes are large 100’s of nm across. This trend was also observed in the XRD, the 18.25° (in 2 theta) or the 001 plane represents the stacking plane or the edge planes.
of TiS₂. From the diffraction pattern the 001 plane is broad with low intensity, indicating very low stacking or small number of edge planes. Whereas the diffraction peak at 40.04° (in 2 theta) or the 011 and 101 planes have a diffraction peak that is much higher in intensity and smaller FWHM. The higher intensity and shaper peak indicate a much larger plane in the crystal. The data indicates that the basal plane in the crystal is much larger than the edge planes (or stacking). Figure 2 C shows the EDS spectrum collected from the sample, which indicates the presence of carbon, oxygen, sulfur, chlorine, and titanium. The presence of carbon, oxygen, and chlorine in low amounts in the sample are not surprising, due to the synthesis conditions: a solvothermal reaction using titanium(IV) chloride elemental sulfur, and a high boiling point carbon based solvent. The presence of the oxygen in the sample may be due to the washing procedure and adsorption of oxygen onto the surface of the TiS₂.

3.3 pH Batch Study:

The binding of Cu²⁺ and Pb²⁺ onto the TiS₂ nanomaterial from pH 2 to pH 6 is presented in Figure 3. As can be seen in Figure 3, the sorption of Cu²⁺ at pH 2 was approximately 100% and decreases to 55% binding at pH 3. There was a significant decrease in the binding of Cu²⁺ onto TiS₂ nanoparticles moving from pH 2 to pH 3. In general, as the pH increased, the binding of Cu²⁺ ions was observed to decreased continually to approximately 10% binding observed at pH 6. A similar trend was observed for the sorption of Pb²⁺ ions onto the TiS₂ nanomaterial. The binding was observed to be approximately 100% at pH 2 and decrease steadily to approximately 60% binding at pH 6. pH 2 was chosen as the optimal binding pH for adsorption due to the highest removal of both metal ions was observed at this pH. The binding results of the present study show an opposite trend compared to many of the results in the literature with other
materials [1,5, 15-16, 29, 30]. For instance, the sorption of Cu\(^{2+}\) onto graphene oxide increased as the initial pH of the solution increased from pH 1 to pH 7 [5]. The binding of Cu\(^{2+}\) and Pb\(^{2+}\) using pristine biochar started below 20% binding at pH 2 and increased to approximately 90% binding at pH 7, whereas engineered biochar reached 100% removal for both Cu\(^{2+}\) and Pb\(^{2+}\) ions at pH 7 [19]. Several other materials have also shown increasing binding with increasing pH, such as: zero valent iron particles, CuO, meranti wood, and graphene oxide nanomaterials [3,5,15-16,18,20]. The removal of Cu\(^{2+}\) and Pb\(^{2+}\) was studied using CuO, Fe\(_3\)O\(_4\), and ZnO nanomaterials by Mahdavi et al.[18]. The results from Mahdavi et al., showed the binding of both Cu\(^{2+}\) and Pb\(^{2+}\) with Fe\(_3\)O\(_4\) and CuO increased with increasing pH, whereas the binding of both ions with ZnO was observed to be pH independent and remained constant throughout the study [18]. In a separate study, also by Mahdavi et al. showed an increase in the binding of Cu\(^{2+}\) and Pb\(^{2+}\) to TiO\(_2\) and Al\(_2\)O\(_3\) nano-adsorbents as the pH of the solution was increased [31]. However, the sorption of both Cu\(^{2+}\) and Pb\(^{2+}\) ions with MgO was not affected when the pH was varied between pH 2 and 7 [31]. Similarly, the sorption of Cu\(^{2+}\) to Fe\(_7\)S\(_8\) was observed to be pH independent with 100% binding occurring from pH 2 to 6, whereas the binding of Pb\(^{2+}\) was observed to increase as the pH of the solution increased [32]. Tamez et al., showed an increasing binding trend for the sorption of Cu\(^{2+}\) and Pb\(^{2+}\) with Fe\(_3\)O\(_4\) as the pH increased from pH 2 to 6 [1]. Similarly, the sorption of Cu\(^{2+}\) with Fe\(_2\)O\(_3\) showed an increase in binding from pH 2 to 6; however, the binding of Pb\(^{2+}\) with the same nanomaterial showed an initial increase from pH2 through 4 and decreased in binding as pH increased to pH 6 [1]. As mentioned earlier, the binding of both the Cu\(^{2+}\) and Pb\(^{2+}\) to the TiS\(_2\) nanomaterial followed an opposite binding trend decreasing with increasing pH. There are several common factors involved in the binding/sorption of metal ions to adsorbents, such as surface charge, ion charge, the availability
of binding sites, which can be related to dissociation constants. Also, the ion affinity and ability to form bonds with surface groups plays a crucial role in adsorption. Within the present study the ability of Cu$^{2+}$ and Pb$^{2+}$ to form metal-sulfur bonds may control the binding of these ions to the TiS$_2$ nanomaterial. Both CuS and PbS are generally formed under acidic conditions as is shown in the literature [32,33]. Low pH for Cu$^{2+}$ and Pb$^{2+}$, sulfur bond formation could translate to higher binding or removal under acidic conditions. The observed higher binding in the presence study may be indicating that the interaction between the Cu$^{2+}$ and Pb$^{2+}$ ions with the TiS$_2$ is the formation of a chemical bond not just through physical sorption.

3.4 Capacitance and Thermodynamics Study:

The results for the sorption/isotherm studies for Cu$^{2+}$ and Pb$^{2+}$ binding to the TiS$_2$ nanomaterial after a 1 hr contact time at 4°C, 22°C, and 45°C are shown in Figure 4. The binding for both ions was determined to follow the Langmuir isotherm model. The linearized Langmuir isotherms are shown in Figure 4, with the associated linear fitting. Figure 4 A shows the binding of the Pb$^{2+}$ ions to the TiS$_2$ nanomaterial and Figure 4B shows the Cu$^{2+}$ binding to the TiS$_2$ nanomaterial. In addition, the correlation coefficients ($R^2$) for the fittings are also shown in Figure 4, which were for the most part are 0.99 or better. The exception being the 20°C isotherm for the binding of the Pb$^{2+}$ to the TiS$_2$ nanomaterial. The Langmuir isotherm was determined to be the isotherm based on the goodness of fit between the model and the data. The Langmuir isotherm defined for the adsorption of a monolayer and linear form of the model is shown below in Eq. (1):

$$\frac{1}{q_e} = \frac{1}{q_m} + \frac{1}{K_a q_m C_e}$$

(1)
Where $q_e$ is the amount of sorbate bound to the sorbent (mg/g), $q_m$ is the maximum binding capacity (mg/g), $K_a$ is a constant, $C_e$ is the equilibrium concentration of the solution.

As can be seen in Table 2, the capacity of the nanomaterial for the sorption of Cu$^{2+}$ starts at 244 mg/g (3.84 mmol/g) at 4°C and decreases with an increasing temperature. At 45°C, the sorption for Cu$^{2+}$ was at 154 mg/g (2.42 mmol/g). On the other hand, the capacity for Pb$^{2+}$ at 4°C was 32 mg/g (0.16 mmol/g) and was observed to increase to 357 mg/g (1.72 mmol/g) at 45°C. The decrease in capacity of the TiS$_2$ for Cu$^{2+}$ as the temperature increased, is indicative of an exothermic reaction occurring whereas the increase in capacity for Pb$^{2+}$ indicates an endothermic process for the binding.

The adsorption capacities observed for the binding of Cu$^{2+}$ and Pb$^{2+}$ with other nano-adsorbents are presented in Table 3. For example, Fe-water treated residues have shown binding capacities of 6 mg/g and 22 mg/g for Cu$^{2+}$ and Pb$^{2+}$, respectively [34]. Additionally, graphene oxide has proved to have high sorption capacities of 530, 345, 294, and 1119 mg/g for Cd$^{2+}$, Zn$^{2+}$, Cu$^{2+}$, and Pb$^{2+}$, respectively [16]. Red mud and activated carbon from pinecones have exhibited similar binding trends [35,36]. Mahdavi et al., showed that TiO$_2$ had binding capacities of 50.2 mg/g and 21.7 mg/g for the sorption of Cu$^{2+}$ and Pb$^{2+}$ [31]. Except for graphene oxide, the binding capacity of TiS$_2$ for Cu$^{2+}$ and Pb$^{2+}$ ions are comparable to the literature values. In fact, in many cases, the binding capacity of TiS$_2$ for Cu$^{2+}$ and Pb$^{2+}$ ions to are higher than the literature values for other materials. The higher binding capacities indicate a stronger interaction between Cu$^{2+}$ and Pb$^{2+}$ ions and the TiS$_2$.

The thermodynamics study was performed in conjunction with the binding capacity study, the data from the isotherm studies was used for the determination of the thermodynamics of the binding process. From the isotherm data performed at different temperatures the Gibbs
free energy, enthalpy, and entropy can be determined and are shown in Table 4. The relationships between thermodynamic parameters and the adsorption isotherms are shown below in Eqs. (2) and (3).

$$\Delta G = -RT \ln k_d$$  \hspace{1cm} (2) \\
$$\ln(k_d) = \frac{\Delta S}{R} - \frac{\Delta H}{RT}$$  \hspace{1cm} (3)

Where $\Delta G$ is the change in Gibbs free energy, $R$ is the gas constant (8.314 J mol$^{-1}$ K$^{-1}$), $T$ is the temperature in Kelvin, $K_d$ is the distribution coefficient, $\Delta H$ is the change in enthalpy, and $\Delta S$ is the change in entropy. $\Delta G$ was determined for both Cu$^{2+}$ and Pb$^{2+}$ at all three temperatures, using eq 2. Whereas $\Delta H$ and $\Delta S$ were determined graphically by plotting $\ln K_d$ vs $1/T$ (in K). A plot of $\ln K_d$ vs $1/T$ (in K) has a slope that is related to $\Delta H$ and an intercept, which is related to $\Delta S$.

The thermodynamic plots for the binding data shown in Figure 5. In addition, the thermodynamic parameters for the sorption process for both ions are presented in Table 4.

According to the results, $\Delta G$ for the sorption of Cu$^{2+}$ with TiS$_2$ ranged from -0.003 kJ/mol to 2.00 kJ/mol from 4°C to 45°C. The data indicates that the reaction was near equilibrium at 4°C and becomes non-spontaneous at higher temperatures. Whereas $\Delta G$ for the sorption of Pb$^{2+}$ onto the TiS$_2$ was observed to range from -2.55 kJ/mol to -16.33 kJ/mol from 4°C to 45°C, which indicates that the sorption process becomes more spontaneous as the temperature increases. In a previous study conducted by Rafiq et al., the sorption of Cu$^{2+}$ with MgO was spontaneous and near equilibrium with temperature ranges from 323-343 K with $\Delta G$ values from -0.35 to -3.26 kJ/mol [37]. Similarly, the sorption of Cu$^{2+}$ with ZnO was spontaneous at the same temperatures.
with ΔG values of -94.43 to -95.37 kJ/mol, respectively [37]. Additionally, Ben-Ali et al., showed that the sorption of Cu^{2+} with pomegranate peel at high temperatures was spontaneous with ΔG values of -5.358 kJ/mol and -7.409 kJ/mol at 303 K and 313 K, respectively [38]. Kumar et al., showed that ΔG for the binding of Pb^{2+} with ZnO nanorods was -8.41, -9.42, and -10.07 kJ/mol at 303 K, 313 K, and 323 K respectively [39]. Furthermore, in a study conducted by Sonmezay et al., ΔG for the sorption of Cu^{2+} with manganese oxide minerals was -27.69, -28.81, and -29.84 kJ/mol at 298, 308, and 318 K, respectively [40]. Zou et al., showed that ΔG for the binding of both Cu^{2+} and Pb^{2+} onto manganese oxide coated zeolite was -50.5, -53.5, and -56.5 kJ/mol and -50.5, -53.6, and -56.7 kJ/mol, respectively at 288, 303, and 313 K [41]. Zepeda et al., showed that the reaction between Cu^{2+} and SnO_2 was non-spontaneous at low temperatures and spontaneous at high temperatures with ΔG values ranging from 3.13 kJ/mol to -0.86 kJ/mol with temperatures ranging from 4°C to 45°C, respectively [42]. The data presented in the current study are within range and are comparable to the data presented in similar studies [37-42]. However, the opposing trend in the binding of the Cu^{2+} ion and Pb^{2+} ions observed with the TiS_2 material has not been observed in many studies. As previously mentioned, the Cu^{2+} ion decreases in binding with increasing temperature, this indicates an exothermic process involved in the binding. Whereas the binding of the Pb^{2+} ions increased with increasing temperature to the TiS_2 indicates an endothermic binding process was occurring. The explanation for these opposing binding processes can explained from the thermodynamic data for compound (for PbS and CuS) formation. The ΔG°f’s for both the copper and Pb sulfides are -53.6 kJ/mol and -98.7 kJ/mol, respectively [43]. The thermodynamic data for the formation of CuS and PbS, indicates the PbS reaction is more favorable than CuS. The more favorable formation of the PbS is indicated by the much larger negative value of ΔG°f observed for PbS compared with the ΔG°f
for CuS. Furthermore, the entropy of formation for PbS (91.2 J/molK) is also larger than the entropy of formation for CuS (66.5 J/molK). Given the combination of processes involved in the binding of both Cu$^{2+}$ and Pb$^{2+}$, along with the favorable formation of the PbS over CuS, it is not surprising that the thermodynamics of binding is more favorable with Pb$^{2+}$ to TiS$_2$ than Cu$^{2+}$ to TiS$_2$. The thermodynamics of compound formation for the PbS and CuS are exemplified in the diffraction patterns shown in Figure 6. The diffraction pattern for the reaction between the Cu$^{2+}$ and the TiS$_2$ (Figure 6 A), which shows no change in the diffraction pattern from that observed for pure TiS$_2$ (shown in Figure 1). However, the Pb$^{2+}$ ion reaction with the TiS$_2$ nanomaterial shows the development of new diffraction peaks in the pattern. The new diffraction peaks shown in Figure 6 B are the diffraction peaks for galena or PbS, this indicates the formation of PbS after reaction [28]. The new diffraction peaks correspond to the PbS 111 (30.51°), an increase in the sized of the diffraction peak at 35.37°, when compared to TiS$_2$ diffraction pattern (the PbS 200 shows at this angle), the PbS 220 (50.89°), and PbS 311 (60.55°). The fitting of the copper binding to the TiS$_2$ material had a reduced $\chi^2$ of 1.72, and the fitting of the TiS$_2$ reacted with the PbS has a $\chi^2$ of 3.56. Both these fitting show good agreement between the data and the fitting.

As previously mentioned, $\Delta S$ and $\Delta H$ were calculated by plotting Ln$K_d$ against $1/T$ (in K) as shown in Figure 6. $\Delta H$ was determined from the slope of the line whereas $\Delta S$ was calculated using the intercept of the plot. According to the results shown in Table 4, $\Delta H$ for the binding of Cu$^{2+}$ was -14.24 kJ/mol indicating an exothermic process occurring during the sorption of Cu$^{2+}$ with TiS$_2$. On the other hand, the value of $\Delta H$ for the sorption of Pb$^{2+}$ was 95.8 kJ/mol indicating that an endothermic process occurs for Pb$^{2+}$ binding to the TiS$_2$. Zepeda et al., showed a $\Delta H$ of 28.73 kJ/mol for sorption of Cu$^{2+}$ with SnO$_2$ nanoparticles indicating an endothermic reaction [42]. Similarly, in a previous study by Cantu et al., showed that the reactions of Cu$^{2+}$ and Pb$^{2+}$
18

with Fe₇S₈ were endothermic with ΔH values of 153.51 kJ/mol and 55.81 kJ/mol, respectively [23]. In addition, the magnitude of ΔH, the binding for Cu²⁺ indicates that a reaction occurs thorough ion exchange whereas Pb²⁺ binding occurs via chemisorption. According to the literature, the sorption processes with ΔH ranging from 8.0 to 16.0 kJ/mol correspond to ion exchange whereas ΔH values greater than 40 kJ/mol are attributed to chemisorption which supports the formation of a PbS compound after sorption, [44]. For chemisorption, the formation of a chemical bond occurs between the adsorbate and adsorbent, which is shown in Figure 6B the formation of the PbS after reaction between Pb²⁺ with the TiS₂.

3.5 Kinetics Study:

The results for the kinetics study for the sorption of Cu²⁺ and Pb²⁺ to TiS₂ nanomaterial are shown in Figure 7. Figure 7A shows the kinetics for the binding of Cu²⁺ ions to the TiS₂ nanomaterial. Whereas Figure 7 B shows the kinetics for the binding of the Pb²⁺ ions to the TiS₂ nanomaterial. The respective equations for the curve fittings and correlation coefficients for each curve fitting are also provided in Figure 7. As shown in Figure 7, the sorption of Cu²⁺ and Pb²⁺ with the TiS₂ nanoparticles was found to follow a zeroth order kinetics model, all the correlation coefficients, R², were observed to range from 0.98 to 1.0. The zeroth order reaction was chosen due to plotting of the concentration against time gave a straight line. A zeroth order kinetics model indicates that the sorption of each of the metal ions is dependent on the contact time with the TiS₂ nanoparticles. The zeroth order reaction model equation is given in Eq. (4).

\[ [C] = k[t] \]  \hspace{1cm} (4)

Where C is the concentration of the ions at any given time, t, is the adsorption time in minutes, and k is the rate constant for the metal-ion adsorption onto the nano-sorbent at equilibrium. The zeroth order kinetic model has been found to fit with many adsorption studies [31, 42, 45, 46].
While other studies investigating the sorption of Cu$^{2+}$ and Pb$^{2+}$ with nanomaterials have shown a pseudo-second order kinetics model can also be suitable [15-16, 18, 41, 47].

From the kinetics data the activation energies for the binding of both Cu$^{2+}$ and Pb$^{2+}$ ions were determined. By performing the kinetics studies at three different temperatures. The activation energy was determined using Arrhenius equation given in eq. (5).

\[
\ln(k) = -\frac{E_a}{RT} - \ln(A)
\]  

(5)

Where \(\ln(k)\) is the natural log of the rate constant; \(E_a\) is the activation energy; \(R\) is the gas constant (8.314 J/mol K); \(T\) is the temperature in Kelvin; \(\ln(A)\) is the frequency factor for the reaction. The Arrhenius plot was constructed by plotting \(\ln(k)\) vs \(1/T\) in Kelvin and is shown in Figure 8. From the Arrhenius the slope of the line in the plot is equal to \(-E_a/R\). The study shows activation energies of 19.7 and 54.1 kJ/mol for the binding of Cu$^{2+}$ and Pb$^{2+}$, respectively as shown in Table 5. Studies have shown that the type of adsorption can be identified based on the magnitude of the activation energy, where energies below 20 kJ/mol are indicative of physisorption [48-50]. Sorption reactions with activation energies found to range from 20 to 80 kJ/mol are indicative of chemisorption [48-50]. Based on the results, the sorption for Pb$^{2+}$ ions occur through chemisorption since the activation energies are clearly above 20 kJ/mol [48-50]. Whereas the binding of the Cu$^{2+}$ ions occurs through a combination of both physisorption and chemisorption process, the activation energy for the binding was close to 20 kJ/mol. These different adsorption mechanisms could be related to the less thermodynamically favorable formation of the Cu-S bonds as mentioned earlier and shown in Figure 6.

3.6 Interference Study:
Figure 9 A, B, and C show the results for the individual interference and combination interferences studies for the sorption of Cu$^{2+}$ and Pb$^{2+}$ to the TiS$_2$ nanomaterial. Common hard cations found in natural water systems (Na$^+$, K$^+$, Ca$^{2+}$, and Mg$^{2+}$) were used as possible interference ions for the sorption of both Cu$^{2+}$ and Pb$^{2+}$ to the TiS$_2$ nanomaterial. The sorption results of Cu$^{2+}$ in the presence of Na$^+$ (Figure 9 A) showed no effect at low concentrations and remained constant at 100% binding. However, in the presence of 1000 ppm Na$^+$, the binding was observed to decrease to approximately 50%. A similar trend was observed in the presence of K$^+$ and Ca$^{2+}$ in which the binding decreased to 60% in the presence of 1000 ppm K$^+$ and 60% binding with 300 ppm Ca$^{2+}$. Mg$^{2+}$ ions on the other hand, show no effect at low concentration but at intermediate and high concentrations, the binding of the Cu$^{2+}$ ions were observed to decrease with increasing concentrations above 3 ppm. At high concentrations, the presence 1000 ppm of Mg$^{2+}$ decreased the Cu$^{2+}$ binding from 100% to 45%. In a study conducted by Tamez et al., the presence of the combined interferences, showed no interference in the binding of Cu$^{2+}$ with Fe$_3$O$_4$ nanomaterial [1]. However, in the same study, the presence of Mg$^{2+}$ caused an antagonistic effect on the binding of Cu$^{2+}$ with Fe$_2$O$_3$ nanomaterial as the concentration of the Mg$^{2+}$ increased [1]. A study by Cantu et al., showed that the increase in concentration of the interfering cations resulted in an antagonistic effect on the binding of Cu$^{2+}$ with Fe$_7$S$_8$.

As seen in Figure 9 B, the presence of any of the cation interferences had a little or no effect on the binding of Pb$^{2+}$ to the TiS$_2$ nanomaterial. Even in the presence of increasing interference concentrations up to 1000 ppm no decrease in binding was observed for Pb$^{2+}$. Tamez et al., also observed a similar trend with the binding of Pb$^{2+}$ in the presence of Na$^+$, K$^+$, Mg$^{2+}$, or Ca$^{2+}$ with an Fe$_3$O$_4$ adsorbent [1]. The presence of Na$^+$ or Ca$^{2+}$ was observed to have a synergistic effect on the sorption of Pb$^{2+}$ with Fe$_2$O$_3$. An increase in Na$^+$ or Ca$^{2+}$ concentration
was observed to cause an increase in the sorption of Pb\(^{2+}\) [1]. Similarly, the results by Cantu et al., showed that for the sorption of Pb\(^{2+}\) onto Fe\(_7\)S\(_8\), little to no effect in the ion binding was observed as the concentration of the cations were increased [31].

The results of the combined interference study are shown in Figure 9 C. As can be seen in Figure 9 C, the Cu\(^{2+}\) binding low and appeared to be concentration independent. The binding of Cu\(^{2+}\) in the combined interference study shown erratic behavior with no observable trend. The Cu\(^{2+}\) ions were observed to bind from approximately 30% to up to a maximum of approximately 60%. However, the binding of Lead was unaffected in the presence of the hard cations ions. The Pb\(^{2+}\) binding was maintained at approximately 100% even in the presence of 1000 ppm of combined interference concentration (the solution contained 1000 ppm of each interferences Na, K, Ca, and Mg). The combined interference data indicates that there is some preferential binding for both Cu\(^{2+}\) ion and Pb\(^{2+}\) ions to the TiS\(_2\) nanomaterial, which would indicate chemisorption is involved in the binding process for both ions. The preferred binding is indicated by the binding data at 300 ppb of either Cu\(^{2+}\) or Pb\(^{2+}\) and 4000 ppm total ion concentration the heavy metals bound to the nanomaterial. The solutions have Pb\(^{2+}\) and Cu\(^{2+}\) molar ratio to interfering ions of 1:2035 and 1:6635, respectively. At such a high molar ratio interference to Pb\(^{2+}\) and Cu\(^{2+}\) the metal ion binding should be eliminated. However, the selectivity in the binding comes from the determined binding mechanism chemisorption for Pb\(^{2+}\) and a combination of physisorption and chemisorption for Cu\(^{2+}\) ions. Physisorption or ion exchange mechanisms would be overcome by the high concentrations of hard cations and the binding of the Pb\(^{2+}\) and Cu\(^{2+}\) would be eliminated.

4.0 Conclusions
The sorption of both Cu$^{2+}$ and Pb$^{2+}$ with the TiS$_2$ nanomaterial was determined to be pH dependent, with both ions binding high at low pH and decreasing with increasing pH. The adsorption capacity for Cu$^{2+}$ was observed to decrease as the temperature increased indicating an exothermic reaction, whereas Pb$^{2+}$ binding capacity was observed to increase as the reaction temperature increased indicating an endothermic reaction. The thermodynamic data in the present study showed the sorption of Cu$^{2+}$ with TiS$_2$ was non-spontaneous and exothermic. However, the Pb$^{2+}$ binding to the TiS$_2$ was spontaneous at all temperatures studied and was an endothermic process. The kinetics data for the sorption of both Cu$^{2+}$ and Pb$^{2+}$ were determined to follow a zeroth order kinetic model, which indicates a direct relationship between the reaction concentration and contact time. In addition, the data indicates the binding occurs through a combination of chemisorption and physisorption for Cu$^{2+}$ binding. Pb$^{2+}$ was determined to bind through chemisorption only. High concentrations of the hard cation interfering species were only observed to decrease the binding of Cu$^{2+}$ and had no effect on the Pb$^{2+}$ binding.

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References:


45. S. Luther, N. Brogfed, J. Kim, J.G. Parsons, Study of the thermodynamics of chromium(III) and chromium(VI) binding to iron(II/III) oxide or magnetite or ferrite and manganese(II) iron (III) oxide or jacobsite or manganese ferrite nanoparticles, J. Colloid Interface Sci. 400( (2013) 97–103.


Figure Legends:

Figure 1: X-ray diffraction pattern for the synthesized TiS$_2$ nanomaterial.

Figure 2: A. SEM image of the synthesized TiS$_2$ nanomaterial, taken at 1000 x magnification. B. SEM image of the synthesized TiS$_2$ nanomaterial, taken at 20000 x magnification. C. EDS spectrum recorded for the TiS$_2$ as synthesized material.
Figure 3: pH profile for the sorption of Cu\textsuperscript{2+} and Pb\textsuperscript{2+} with the TiS\textsubscript{2} nano-sorbent ranging from pH 2 to pH 6.
Figure 4: Linearized Langmuir isotherm plots for the binding of Pb\textsuperscript{2+} ions to the TiS\textsubscript{2} nanoparticles at 4 °C, 20°C, 45°C (A) and the binding of Cu\textsuperscript{2+} ions to the TiS\textsubscript{2} nanomaterial at 4 °C, 20°C, and 45°C (B).
Figure 4
Figure 5: Thermodynamic plot for the sorption of Cu$^{2+}$ and Pb$^{2+}$ with the TiS$_2$ nano-sorbent.

Figure 6: X-ray diffraction pattern of the TiS$_2$ nanomaterial after reaction with Cu$^{2+}$ ions (A) and Pb$^{2+}$ ions (B).
Figure 6
Figure 7: Kinetics plots for the reaction for Cu$^{2+}$ (A) and Pb$^{2+}$ (B) with the synthesized TiS$_2$ nanomaterial at temperatures of 4, 20, and 45°C.
Figure 7
Figure 8: Arrhenius plot for the sorption of Cu$^{2+}$ and Pb$^{2+}$ with the TiS$_2$ nano-sorbent.
Figure 9: A) Sorption of Cu\(^{2+}\) to the TiS\(_2\) nano-sorbent with individual cationic interfering species, B) sorption of Pb\(^{2+}\) to the TiS\(_2\) nano-sorbent with individual cationic interfering species. C. Sorption of Cu\(^{2+}\) and Pb\(^{2+}\) to the TiS\(_2\) nano-sorbent in the presence of combined cationic interfering species.
Table 1: ICP-OES parameters for the analysis of Cu^{2+} and Pb^{2+} solutions after equilibration with the TiS_{2} nanomaterial.

<table>
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<tr>
<th>Parameter</th>
<th>Settings</th>
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<tr>
<td>( \lambda_{Cu} )</td>
<td>327.393 nm</td>
</tr>
<tr>
<td>( \lambda_{Pb} )</td>
<td>217 nm</td>
</tr>
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<td>RF power</td>
<td>1500 W</td>
</tr>
<tr>
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<td>Gemcone (low flow)</td>
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<td>Plasma Flow</td>
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<td>Auxiliary Flow</td>
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<td>Spray Chamber</td>
<td>Cyclonic</td>
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<tr>
<td>Integration Time</td>
<td>20 seconds</td>
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<td>Replicates</td>
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</tbody>
</table>

Table 2: Binding capacities for the binding of Cu^{2+} and Pb^{2+} onto the TiS_{2} nanomaterial at various temperatures.

<table>
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<th>Ion</th>
<th>T (K)</th>
<th>Capacity (mg/g)</th>
<th>Capacity (mmol/g)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Pb^{2+}</td>
<td>277 K</td>
<td>32</td>
<td>0.16</td>
</tr>
<tr>
<td></td>
<td>295 K</td>
<td>166</td>
<td>0.80</td>
</tr>
<tr>
<td></td>
<td>318 K</td>
<td>357</td>
<td>1.72</td>
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<td>Cu^{2+}</td>
<td>277 K</td>
<td>244</td>
<td>3.83</td>
</tr>
<tr>
<td></td>
<td>295 K</td>
<td>222</td>
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</tr>
<tr>
<td></td>
<td>318 K</td>
<td>154</td>
<td>2.42</td>
</tr>
</tbody>
</table>
Table 3: Adsorption capacities for the binding of Cu\(^{2+}\) and Pb\(^{2+}\) to different nano-adsorbents.

<table>
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<th>Material</th>
<th>Ion</th>
<th>Capacity (mmol/g)</th>
<th>Capacity (mg/g)</th>
<th>Reference</th>
</tr>
</thead>
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<td>Fe(_2)O(_3)</td>
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<td>Pb(^{2+})</td>
<td>0.31</td>
<td>47.62</td>
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<td>0.58</td>
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<td>Graphene Oxide</td>
<td>Cu(^{2+})</td>
<td>1.84</td>
<td>117.5</td>
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<td>Fe(_3)O(_4)</td>
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<td>0.49</td>
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<td>ZnO</td>
<td>Cu(^{2+})</td>
<td>0.54</td>
<td>137.5</td>
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<td>ZnO</td>
<td>Pb(^{2+})</td>
<td>2.16</td>
<td>112.7</td>
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<tr>
<td>CuO</td>
<td>Cu(^{2+})</td>
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Table 4: Thermodynamic parameters for the sorption of Cu$^{2+}$ and Pb$^{2+}$ with the TiS$_2$ nanomaterial.

<table>
<thead>
<tr>
<th>Ion</th>
<th>$\Delta G$ (kJ/mol)</th>
<th>$\Delta H$ (kJ/mol)</th>
<th>$\Delta S$ (J/mol)</th>
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<tbody>
<tr>
<td>Pb$^{2+}$</td>
<td>-2.55 (277 K)</td>
<td>-10.68 (298 K)</td>
<td>95.8</td>
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<td>-16.33 (318 K)</td>
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<td>355.8</td>
</tr>
<tr>
<td>Cu$^{2+}$</td>
<td>-0.003 (277 K)</td>
<td>1.10 (298 K)</td>
<td>-14.24</td>
</tr>
<tr>
<td></td>
<td>2.00 (318 K)</td>
<td></td>
<td>-54.1</td>
</tr>
</tbody>
</table>

Table 5: Results for the kinetics study showing the calculated activation energies for the sorption of Cu$^{2+}$ and Pb$^{2+}$ to the TiS$_2$ nanomaterial.

<table>
<thead>
<tr>
<th>Ion</th>
<th>T (K)</th>
<th>$E_a$ (kJ/mol)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Pb$^{2+}$</td>
<td>277</td>
<td>54.1</td>
</tr>
<tr>
<td></td>
<td>296</td>
<td></td>
</tr>
<tr>
<td></td>
<td>318</td>
<td></td>
</tr>
<tr>
<td>Cu$^{2+}$</td>
<td>277</td>
<td>19.7</td>
</tr>
<tr>
<td></td>
<td>296</td>
<td></td>
</tr>
<tr>
<td></td>
<td>318</td>
<td></td>
</tr>
</tbody>
</table>